# How to Support the Government Procurement by a Pairwise Comparisons Model

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**Abstract** This study demonstrates how a government procurement process could be improved by the pairwise comparisons method. A case study, related to assessment of project proposals is used for demonstration purpose. The project proposals were requested by a Canadian government agency to assess the environmental and public safety hazards of abandoned mines. However, the presented model is applicable (with easy-to-implement modifications) to any other case of government procurement.

Keywords government procurement  $\cdot$  project proposal assessment  $\cdot$  pairwise comparison  $\cdot$  distance-based inconsistency  $\cdot$  convergence  $\cdot$  knowledge management

## **1** Introduction

Government procurement, also called public tendering or public procurement, is the procurement of goods and services on behalf of a public authority, such

Alphabetical order implies equal contribution

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R.Tadeusiewicz AGH, Krakow, Poland as a government agency. According to [20], it accounts for more than EUR 2 trillion, or 18% of the EU GDP and it is a substantial part of the global economy. Evidently, government procurement is important to the EU economy as the "new EU-rules on public procurement" have been recently updated.

Laws of most countries regulates government procurement to prevent fraud, waste, corruption or local protectionism. It usually requires the procuring authority to issue public tenders if the value of the procurement exceeds a certain threshold. In the USA, the principal set of rules [22] is the Federal Acquisition Regulation System. Government procurement in the European Union has been regulated and harmonized by laws since the 1970s. In Poland, government procurement is regulated by the Public Procurement Law, an act of parliament of 29 January 2004 (see [19]). However, government procurement in Poland accounts for only 8% of GNP and it is less than 18% of the EU average.

The most recent events related to public procurement in Poland are living testimony that the "legal solution" is not efficient. Evidently, there is a need for additional research of applied nature since the strict sciences have mostly been focused on processing quantitative (or objective) data than qualitative (subjective) data, which we use more frequently in daily life. The importance of subjectivity processing is expressed by the idea of *bounded rationality*, proposed by Herbert A. Simon (a Nobel prize winner), as an alternative basis for the mathematical modeling of decision making.

Objective (or measurable by instruments) data, perceived as precise data, are always preferred over subjective data. Subjective data are often based on professional knowledge, experience, or even feelings. In general, they are not regarded as precise as the measurable objective data. The lack of proper methods for processing subjectivity adds to the problem. However, objectivity is often illusive since there is a fine line between objectivity and subjectivity, more often than we realize it. For example, let us assume that a contractor hopes for \$1,000 for his/her service. A customer might put forward a slightly lower offer, such as \$999 and the seller would most likely accept. If it is accepted, the next correction could be \$998. The customer could continue offering a dollar lower, but only to a certain point, because the contractor has his/her own subjective assessment of the offered service. So, what we are really often prepared to accept is highly dependent on our subjective assessment. There are not as many numbers "carved in stone" in real life as we would like to believe.

Assessing environmental damage is expensive and government agencies in Canada must use tendering processes (known as tendering) for the selection of the contractor. Although the concept of the total cost comes into play, other factors such as reliability, quality, flexibility and timing, are considered in the procurement process. Our approach was to compute a proposal quality index to short list them for the final selection by the panel of experts. Pairwise comparisons allow us to express preferences more easily. These preferences can be highly subjective (e.g., likes/dislikes). Pairwise comparisons were most likely used even before numbers were invented. We can easily envision that "weighting" took place during the Stone Age to decide if a fish, in one hand, can be bartered for a bird in the other hand. A comprehensive introduction to pairwise comparisons is in [17]. It includes mathematical basics and can be downloaded for free from http://arxiv.org/abs/1307.6272 repository.

The distance-based inconsistency was introduced in [15] in 1993 and independently analyzed in [4] in 2008. It was validated by numerous practical experimentations.

### 2 Problem definition

The challenge is to select the best proposal, i.e., to choose the most appropriate projects to do a certain task. In our case, it was for the assessment of abandoned mines in a Canadian mining district. We deliberately avoid using "the best" for the selected bid since it calls for the definition of being "the best". Certainly, it indicates "the highest quality of any kind" but within a reason.

About fifty companies submitted their proposals. The information given in the proposals was studied to select the winner, i.e., the company which meets criteria and expectations set by the expert panel called to conduct the selection. For this, we needed to assign a "goodness value" to each proposal and rank all of them using such a value.

We started with a certain number of criteria, proposed by the expert panel from the government agency, which each company should meet to be qualified for the contract. The main problem is to prioritize, i.e., find the contribution of each criterion to the overall score. After a certain number of meetings and discussions with the government agency representatives, the hierarchy (depicted by Fig. 5) was designed.

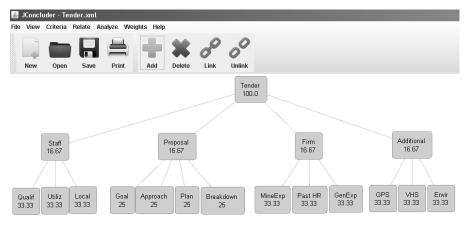


Fig. 1 Tendering process model

The lowest hierarchy level in Fig.1 consists of thirteen criteria Subsequently, we would need to assign the priority (the weight) to each criterion by comparing them in pairs. However, the number of all pairs criteria is 78 (13 \* (13 - 1)/2) and too large for comparing them. For this reason we cluster similar criteria to built the next higher level of the hierarchy. Groups of criteria are compared in pairs. We divided the criteria into four groups:

- 1. "staff" (to be assigned by the firm to the project),
- 2. "proposal" (how the firm is going to manage the task),
- 3. "firm" (experience and reputation of the firm),
- 4. "additional qualifications".

Next, the elements in a level are compared against all others in the same level, with respect to the elements on the preceding level. These comparisons are arranged at the table (matrix). Fig. ?? shows a scale assumed for pairwise comparisons. After a number of experiments the following scale seems to be the most effective:

Table 1 Rating scale

Rating scale	meaning
1	equal or uncertain
2	moderate
3	extreme
1.5, 2.5, 2.8	itermediate values
1/x	reciprocal of x

The matrix of pairwise comparisons is constructed by comparing criteria in pairs according to their relative importance. Say that "staff" is moderately more important (according to the expert panel subjective assessment) than "proposal", then we would place a "3" in the entry (row-staff,columnproposal). Say, that we assess the group staff to be by far more important than group firm, we place a "5" in the entry (row: "staff" and column: "firm"). A similar pairwise comparisons process takes place for all other entries. The system requirement is to fill in only the "upper matrix triangle" (above the main diagonal) of the matrix since the lower triangle is reciprocal  $(a_{ij} = 1/a_{ji})$ . After the expert panel entered its pairwise comparisons, the final results were computed as the geometric means of rows and normalized to 1 as illustrated ???.

#### Table 2 Group 3

Criterion		А	В	С	D	Ε
Cost breakdown	Α	1	1	2	4	5
Goal understanding	В	*	1	1	5	7
Approach	С	*	*	1	7	7
Work plan schedule	D	*	*	*	1	5
Final report design	Е	*	*	*	*	1

Once the matrices in each level are completed, the relative importance of the elements in the level is given by geometric means of rows in the PC

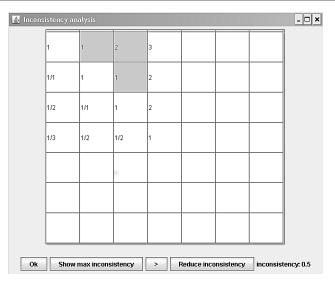


Fig. 2 PC matrix for "staff"

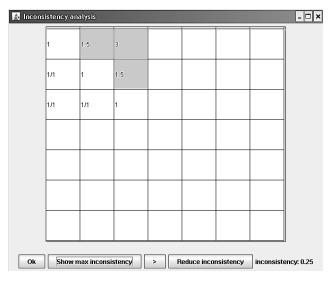


Fig. 3 PC matrix for "proposal"

matrix. The weights are normalized so the sum is equal 100. Thus, we can effectively attribute a percentage of priority to each factor at each level. The priority of each criterion at the lowest (third) level is obtained by multiplying the priority of the criterion under the proper group by the priority of this group. The priorities of all criteria sum up to 100. The results are presented in Fig. ??.

The expert panel evaluated each company in regards to the assumed criterion. They were using the scale from 0 to 7. According to the experts' as-

 ${\bf Table \ 3} \ {\rm Qualification}$ 

Criterion		Α	В	С
GPS experience	Α	1	1	2
Envirn. Knowledge	В	*	1	1
VHS/35mm camera exper.	С	*	*	1

Table 4 Add caption

Project = 1								
Staff=0.568	Proposal=252	Firm=0.120	Additional=059					
Qual=0.649	CostDistr=0.310	PastPr=0.550	GPS = 0.655					
Expl=0.279	Appr=0.287	MineEx=0.368	Envir=0.290					
Person=0.072	Underst=0.286	GenExp=0.082	VHS=0.055					
	Sched=0.081							
	Rep-0.360							

sessments and weights computed by the system the contribution of the first six criteria to the final score was equal 81.7%. We recommended to start the assessment of all proposals using these six criteria. The final results are given below. In the first line we have the weight (priority) of each criterion (in percentage). The first column consists of the total score of the company whose number is given in the second column. The assessment of the company (in the scale from 0 to 7). The last column, named "cost" consists of the costs given by the company.

The general perception was that the estimation process was not only considerably shorter, but also fairer, since the existing panel of experts concentrated its attention on the most important factors of the proposals.

Weights		37	15.9	7.8	7.2	7.2	6.6	4.4	4.1	з.9	2	1.7	ı	D.9	р.з	Rubbab	
Total	#	#1	#2	#3	#4	#5	#6	#7	#8	#9	#1D	#11	#12	#13	#14		Total cost
71.26	16	6.5	6	5.5	6.5	6.5	4	4	7	4.5	з.5	4	5	5	6.3	12.7	\$193,2DD
70.03	21	6	6	6	6.5	5.5	6	5.5	5	D.5	4.5	5.5	5	5	4	10.8	\$152,522
66.26	22	6	5	6	6	5	5.5									D	\$299,74D
63.74	3 D	6	6	4	5.5	4.5	6									D	\$497,4DD
62.96	36	6	3	4	4	3.3	6									D	\$176,7DD
62.74	35	5.5	5.5	6	4.3	5										D	Ş6D3,363
62.66	13	6	з	5.5	6	6	6									D	\$202,837
62.36	37	6	3	з	4.5	5.5	6									D	\$272,D37
62.33	49	5.5	6	3	5.5	4.3	4									D	\$236,39D
61.84	4	6	4	4.3	6	3	5									D	\$173,DDD
6D.44	41	5.5	4	6.3	5	3.3	4.3									D	\$191,D7D
38.04	44	5.5	4	4	5	4.3	6									D	\$338,7DD
36.34	з	5.5	з	6	4	5	5									D	\$246,923
33.71	31	4.5	5	6	4	4	6									D	\$233,27D
34.50	5	5	5	5	4	5	2									D	\$1DD,423
34.41	14	5	4	3.5	5	5	5									D	\$224,88D
53.Dl	48	5.5	2.5	2.5	4.5	5.5	5.5									D	\$82,43D
32.37	47	4.5	4	4.3	4	5.5	3									D	\$4D2,963
31.66	27	4	4	4	5.5	3.3	6									D	\$219,633
42.44	46	3.5	3.5	4.3	4	з	4									D	\$317,D9D
42.11	38	3.5	з	з	4.5	4	3									D	\$196,6DD
40.18	29	4.5	2.5	з	2	1.S	4									D	\$163,DDD
39.68	23	4	4.5	2	2	з	r									D	\$193,8DD
32.76	32	з	2.5	2	з	з	з									D	\$113,55D
30.99	24	2	2.5	5	4	4	г									D	\$221,275
29.97	17	2.5	r	4.5	2.5	3.5	3.5									D	\$468,2DD
29.32	2	2.5	2.5	2	2.5	2	4									D	\$324,947
27.87	77	2.5	2	2	2	2	4									D	\$142,6DD
26.77	6	3.5	г	2	D	Þ	4									D	\$37,62D
25.43	28	2.5	2	1.5	2	2	2									D	\$34D,DDD
17.42	зD	1.5	1.5	г	1.5	1.5	2									D	ŞD
1.11	23	D	D	г	D	D	D									D	ŞSD,DDD
Average		4.38	3.61	3.91	3.94	4	4.23										Ş239,763

Fig. 4 Assessment results

Figure 4 shows the results. The entry "-"means "it does not matter" since it was evident that only the two top contenders had realistic change of winning the competition. Proposals 22 and 50 were too expensive and the difference in the point on criteria C1 to C6 between the winner and project 36 was too big to consider it as a potential winner.

The companies #16 and #21 obtained the best scores: 71.26%, 70.03% (81.7% was the highest possible result according to the first six criteria). The remaining criteria (#7 to #14) confirmed the good position of these two companies. The final choice in favor of the company #21, was the cost they proposed for their services. We can see that criteria from #7 to #14 have turned out to be of lower significance, with each of them below 5% and some even below 1%, which could be treated (from the procurement assessment perspective) as "information noise". In it not really a side product but an important results as such criteria should be dropped from the assessment model in the future. We have included it for illustration purpose.

#	Criteria	R-total
1	Relevant qualification of personnel to be assigned to proj.	37.0
2	Explanation of use of personnel	52.9
3	Costs breakdown	60.7
4	Approach	67.9
5	Goal understanding	75.1
6	Past projects	81.7
7	Experience in mine auditing, hazard identification	86.1
8	Local knowledge of personnel	90.2
9	Experience with GPS system	94.1
10	Work plan schedule	96.1
11	Environmental knowledge and training	97.8
12	General experience	98.8
13	Proposed format of final report	99.7
14	Experience with 35mm cameras and VHS video	100.0

Table 5 Computed weights

#### 3 The inconsistency reduction

Starting with [4], a distance-based adjective has been used by other researchers for the new inconsistency defined in 1993 in [15]. The distance-based adjective reflects the nature of the inconsistency indicator, which is defined as a minimal distance from the nearest consistent triad in matrix A. Matrix A is defined as:

$$A = \begin{pmatrix} 1 & a_{12} \cdots a_{1n} \\ \frac{1}{a_{12}} & 1 \cdots a_{2n} \\ \vdots & \vdots & \vdots \\ \frac{1}{a_{1n}} & \frac{1}{a_{1n}} \cdots & 1 \end{pmatrix}$$

In data and knowledge processing, this is expressed by the popular adage: GIGO (garbage in – garbage out). GIGO summarizes well what has been known for a long time: processing "dirty data" cannot guarantee meaningful results. The distance-based inconsistency allows decision makers to localize the most inconsistent triad (or triads) in their own assessments. It is expressed by the maximum of all triads  $a_{ik}, a_{kj}, a_{ij}$  of elements of A (say, with all indexes i,j,k distinct) of their inconsistency indicators, which in turn are defined as:

$$ii = \min(|1 - \frac{a_{ij}}{a_{ik}a_{kj}}|, |1 - \frac{a_{ik}a_{kj}}{a_{ij}}|).$$
(1)

The process of reducing global inconsistency of a pairwise comparisons matrix (PC matrix), is based on the detection of triads (say,  $\{a_{ik}, a_{kj}, a_{ij}\}$ ) with the maximal inconsistency. When such a triad is located, we modify the value of  $a_{ik}$ ,  $a_{kj}$  or  $a_{ij}$  in order to make the replaced triad fully consistent.

#### 3.1 Approximation of pairwise comparison matrices

The initial PC matrix is not expected to be fully consistent. Solving real-life problems usually involves inconsistent assessments. However, a matrix with a large inconsistency is undesirable according to "the garbage in, garbage out (GIGO)" principle. Inconsistencies often reflect assessing "every criterion being more important than another".

For an inconsistency to occur, a minimum size of 3 for PC matrix is required, since at least one triad needs to exits. Needless to say that for two comparisons, inaccuracy (not inconsistency) takes place. We use n = 7 as the maximal PC matrix size. For a matrix with n elements, there are n\*(n-1)/2comparisons. It gives us 21 comparisons for n = 7 and it is a psychological limit for most respondents to cooperate (we wonder who would agree to compare 100 objects giving 4,950 pair combinations).

## 4 Pairwise comparisons method in the Polish law

This study proposes an improvement to the government procurement using pairwise comparisons. Such an approach has been already used for the assessment of research entities by the Ministerial Commission (the Polish acronym KEJN). The Ministry of Education Bill, dated 2012-07-13, set the criteria and algorithm for categorizing scientific entities. The original Polish text from [26] is depicted by Fig. 5).

(Dz.U. 2012 nr 0 poz. 877):

4. Na podstawie ocen, o których mowa w ust. 1, komisja Komitetu ustala ostateczną ocenę jednostki naukowej w danej GWO, przy zastosowaniu metody porównań parami, wykorzystującej ważoną relację przewyższania, według algorytmu określonego w załączniku nr 8 do rozporządzenia.

Fig. 5 The Polish text of the relevant Ministry Bill fragment

The authors' interpretation (not legally binding hence) of Fig. 5 is as follows:

4. Using assessments set in the part 1 of the Bill, The Ministry Commission sets the category of the scientific entity in a given region by using the pairwise comparisons method. The algorithm for the method is in the Appendix 8.

The pairwise comparisons method has been explicitly used five times in the Ministry Bill.

#### **5** Conclusions

The pairwise comparisons method contributed to shorter processing time of the proposal assessment. There was no single appeal, hence it is safe to assume that the proposed model was a success. In Canada, the government procurement system has been in place for a longer period of time than in Poland. Its perfection has never stopped, which is why it has been possible for our model to be used. The pairwise comparisons method contributed to shorter processing time of the proposal assessment. It provided efficiency, confidence and fairness to the tendering process.

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